Active Shape Model

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* slides credit to Dr. Cootes
Problem Definition

Moving and deforming a **template** to minimize the **distance** between the template and an image.

Note the difference between image alignment and image registration.
Applications

• Face fitting [Baker & Matthews’ 04IJCV]
• Expression analysis/recognition [Zhu & Ji’ 06CVPR]
• Image coding [Baker et al.’ 04PAMI]
• Tracking [Hager & Belhumeur’ 98PAMI]
• Image mosaicing [Shum & Szeliski’ 00IJCV]
• Medical image interpretation [Mitchell et al.’ 02TMI]
• Dynamic texture [Doretto & Soatto’ 06PAMI]
• Industrial inspection [Rolfe et al.’ 01IME]
Active Shape Models

Suppose we have a statistical shape model
• Trained from sets of examples

How do we use it to interpret new images?

Use an “Active Shape Model”

Iterative method of matching model to image
Building Models

Require labelled training images
• landmarks represent correspondences
Building Shape Models

Given aligned shapes, \( \{ \mathbf{x}_i \} \)

Apply PCA

\[
\mathbf{x} = \bar{\mathbf{x}} + \mathbf{Pb}
\]

\( \mathbf{P} \) – First \( t \) eigenvectors of covar. matrix

\( \mathbf{b} \) – Shape model parameters
Hand Shape Model

Varying $b_1$  Varying $b_2$  Varying $b_3$
Active Shape Models

Match shape model to new image

Require:
• Statistical shape model
• Model of image structure at each point
Placing Model in Image

The model points are defined in a model coordinate frame.

Must apply global transformation, $T$, to place in image.

$$x = \bar{x} + P_b$$

$T(x; X_c, Y_c, s, \theta)$

$$X = T(\bar{x} + P_b)$$
Local optimisation

Initialise near target

- Search along profiles for best match, $X'$
- Update parameters to match to $X'$.

$(X_i, Y_i)$
Local Structure Models

Need to search for local match for each point

Model
- Strongest edge
- Correlation
- Statistical model of profile
Computing Normal to Boundary

Tangent \((t_x, t_y)\)

Normal \((n_x, n_y) = (-t_y, t_x)\)

\((X_{i-1}, Y_{i-1})\)

\((X_{i+1}, Y_{i+1})\)

\((t_x, t_y) \approx \frac{(d_x, d_y)}{\sqrt{d_x^2 + d_y^2}}\)

\(d_x = X_{i+1} - X_{i-1}\)

\(d_y = Y_{i+1} - Y_{i-1}\)

(Unit vector)
Sampling Along Profiles

Model boundary

Model point
$(X,Y)$

Profile normal to boundary

Interpolate at these points

$(X,Y) + i(s_n n_x, s_n n_y)$

$i = ... -2, -1, 0, 1, 2, ...$

Take steps of length $s_n$ along $(n_x, n_y)$

$s_n n_x$

$s_n n_y$
Noise Reduction

In noisy images, average orthogonal to profile

- Improves signal-to-noise along profile

Use $g_i = 0.25g_{i1} + 0.5g_{i2} + 0.25g_{i3}$

Sampled profile is $g = (..., g_{-2}, g_{-1}, g_0, g_1, g_2, ...)$
Searching for Strong Edges

Select point along profile at strongest edge

\[
\frac{dg(x)}{dx} = 0.5(g(x+1) - g(x-1))
\]
Profile Models

Sometimes true point not on strongest edge

Model local structure to help locate the point
Statistical Profile Models

Estimate p.d.f. for sample on profile

Normalise to allow for global lighting variations

From training set learn

\[ p(g) \]
Profile Models

For each point in model

• For each training image
  – Sample values along profile
  – Normalise

• Build statistical model
  – eg Gaussian PDF using eigen-model approach
Searching Along Profiles

During search we look along a normal for the best match for each profile.
Search Algorithm

Search along profile

Update global transformation, $T$, and parameters, $b$, to minimise

$$| X - T(\bar{x} + Pb) |^2$$

$(X_i, Y_i)$
Updating Parameters

Find pose and model parameters to minimise

Either

\[ f(b, X_c, Y_c, s, \theta) = \| X - T(\vec{x} + Pb; X_c, Y_c, s, \theta) \|^2 \]

- Put into general optimiser
- Use two stage iterative approach
Updating Parameters

\[ f(b, X_c, Y_c, s, \theta) = \left| X - T(\bar{x} + Pb; X_c, Y_c, s, \theta) \right|^2 \]

Repeat until convergence:
Fix \( b \) and find \((X_c, Y_c, s, \theta)\) which minimise \( \left| X - T(\bar{x} + Pb) \right|^2 \)

Analytic solution exists (see notes)
Fix \((X_c, Y_c, s, \theta)\) and find \( b \) which minimises \( \left| X - T(\bar{x} + Pb) \right|^2 \)

\[ b = P^T (T^{-1}(X) - \bar{x}) \]
Multi-Resolution Search

Train models at each level of pyramid
• Gaussian pyramid with step size 2
• Use same points but different local models

Start search at coarse resolution
• Refine at finer resolution
Lessons learned

ASM is relatively fast

ASM too simplistic; not robust when new images are introduced

May not converge to good solution

Key insight: ASM does not incorporate all gray-level information in parameters
Extensions

Active Appearance Models

Applications
Active Appearance Models (AAM)

Model

“Shape”

“texture”
Shape Models

\[ s = (x_1, y_1, x_2, y_2, \ldots, x_v, y_v)^T. \]

\[ s = s_0 + \sum_{i=1}^{n} p_i s_i. \]
Appearance Models

\[ A(x) = A_0(x) + \sum_{i=1}^{m} \lambda_i A_i(x) \quad \forall x \in s_0 \]
Model Instantiation

Appearance, $A = A_0 + 3559A_1 + 351A_2 - 256A_3 \ldots$

Shape, $s = s_0 - 54s_1 + 10s_2 - 9.1s_3 \ldots$

$W(x; p)$
Fitting AAM

$$\sum_{x \in s_0} \left[ A_0(x) + \sum_{i=1}^{m} \lambda_i A_i(x) - I(W(x; p)) \right]^2$$

Initial: 21.8
3 iterations: 18.0
6 iterations: 11.9
10 iterations: 0.69
15 iterations: 0.09
20 iterations: 0.09
Applications

https://www.youtube.com/watch?v=M1iu__viJN8

https://www.youtube.com/watch?v=rOAcXbLEypU

Hand tracking (MATLAB example)